

Cryptography and Network Security Chapter 5

Fifth Edition
by William Stallings

Lecture slides by Lawrie Brown

Chapter 5 –Advanced Encryption Standard

"It seems very simple."

"It is very simple. But if you don't know what the key is it's virtually indecipherable."

—**Talking to Strange Men, Ruth Rendell**

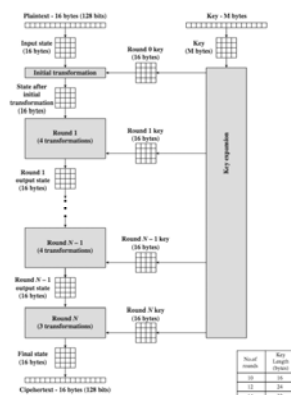
Origins

- clear a replacement for DES was needed
 - have theoretical attacks that can break it
 - have demonstrated exhaustive key search attacks
- can use Triple-DES – but slow, has small blocks
- US NIST issued call for ciphers in 1997
- 15 candidates accepted in Jun 98
- 5 were shortlisted in Aug-99
- Rijndael was selected as the AES in Oct-2000
- issued as FIPS PUB 197 standard in Nov-2001

The AES Cipher - Rijndael

- designed by Rijmen-Daemen in Belgium
- has 128/192/256 bit keys, 128 bit data
- an **iterative** rather than **feistel** cipher
 - processes data as block of 4 columns of 4 bytes
 - operates on entire data block in every round
- designed to be:
 - resistant against known attacks
 - speed and code compactness on many CPUs
 - design simplicity

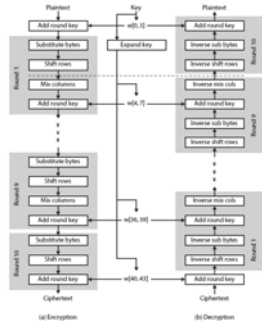
AES Encryption Process



AES Structure

- data block of 4 columns of 4 bytes is state
- key is expanded to array of words
- has 9/11/13 rounds in which state undergoes:
 - byte substitution (1 S-box used on every byte)
 - shift rows (permute bytes between groups/columns)
 - mix columns (subs using matrix multiply of groups)
 - add round key (XOR state with key material)
 - view as alternating XOR key & scramble data bytes
- initial XOR key material & incomplete last round
- with fast XOR & table lookup implementation

AES Structure



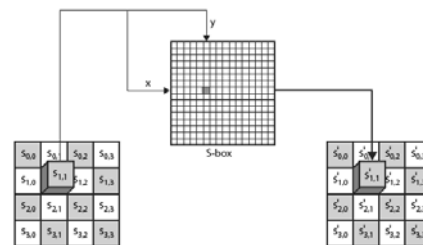
Some Comments on AES

1. an **iterative** rather than **feistel** cipher
2. key expanded into array of 32-bit words
 1. four words form round key in each round
3. 4 different stages are used as shown
4. has a simple structure
5. only AddRoundKey uses key
6. AddRoundKey a form of Vernam cipher
7. each stage is easily reversible
8. decryption uses keys in reverse order
9. decryption does recover plaintext
10. final round has only 3 stages

Substitute Bytes

- a simple substitution of each byte
- uses one table of 16x16 bytes containing a permutation of all 256 8-bit values
- each byte of state is replaced by byte indexed by row (left 4-bits) & column (right 4-bits)
 - eg. byte {95} is replaced by byte in row 9 column 5
 - which has value {2A}
- S-box constructed using defined transformation of values in $GF(2^8)$
- designed to be resistant to all known attacks

Substitute Bytes



Substitute Bytes Example

EA	04	65	85
83	45	5D	96
5C	33	98	B0
F0	2D	AD	C5

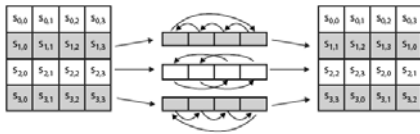
→

87	F2	4D	97
EC	6E	4C	90
4A	C3	46	E7
8C	D8	95	A6

Shift Rows

- a circular byte shift in each each
 - 1st row is unchanged
 - 2nd row does 1 byte circular shift to left
 - 3rd row does 2 byte circular shift to left
 - 4th row does 3 byte circular shift to left
- decrypt inverts using shifts to right
- since state is processed by columns, this step permutes bytes between the columns

Shift Rows



87	F2	4D	97
EC	6E	4C	90
4A	C3	46	E7
8C	D8	95	A6

→

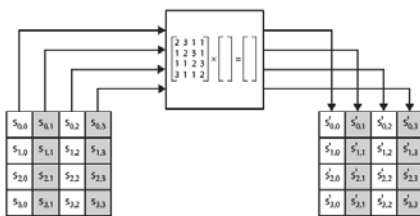
87	F2	4D	97
6E	4C	90	EC
46	E7	4A	C3
A6	8C	D8	95

Mix Columns

- each column is processed separately
- each byte is replaced by a value dependent on all 4 bytes in the column
- effectively a matrix multiplication in $GF(2^8)$ using prime poly $m(x) = x^8 + x^4 + x^3 + x + 1$

$$\begin{bmatrix} 02 & 03 & 01 & 01 \\ 01 & 02 & 03 & 01 \\ 01 & 01 & 02 & 03 \\ 03 & 01 & 01 & 02 \end{bmatrix} \begin{bmatrix} s_{0,0} & s_{0,1} & s_{0,2} & s_{0,3} \\ s_{1,0} & s_{1,1} & s_{1,2} & s_{1,3} \\ s_{2,0} & s_{2,1} & s_{2,2} & s_{2,3} \\ s_{3,0} & s_{3,1} & s_{3,2} & s_{3,3} \end{bmatrix} = \begin{bmatrix} s'_{0,0} & s'_{0,1} & s'_{0,2} & s'_{0,3} \\ s'_{1,0} & s'_{1,1} & s'_{1,2} & s'_{1,3} \\ s'_{2,0} & s'_{2,1} & s'_{2,2} & s'_{2,3} \\ s'_{3,0} & s'_{3,1} & s'_{3,2} & s'_{3,3} \end{bmatrix}$$

Mix Columns



Mix Columns Example

87	F2	4D	97
6E	4C	90	EC
46	E7	4A	C3
A6	8C	D8	95

→

47	40	A3	4C
37	D4	70	9F
94	E4	3A	42
ED	A5	A6	BC

$$\begin{aligned} (\{02\} \cdot \{87\}) \oplus (\{03\} \cdot \{6E\}) \oplus \{46\} \oplus \{A6\} &= \{47\} \\ \{87\} \oplus (\{02\} \cdot \{6E\}) \oplus (\{03\} \cdot \{46\}) \oplus \{A6\} &= \{37\} \\ \{87\} \oplus \{6E\} \oplus (\{02\} \cdot \{46\}) \oplus (\{03\} \cdot \{A6\}) &= \{94\} \\ (\{03\} \cdot \{87\}) \oplus \{6E\} \oplus \{46\} \oplus (\{02\} \cdot \{A6\}) &= \{ED\} \end{aligned}$$

AES Arithmetic

- uses arithmetic in the finite field $GF(2^8)$
- with irreducible polynomial

$$m(x) = x^8 + x^4 + x^3 + x + 1$$
 which is (100011011) or {11b}
- e.g.

$$\{02\} \cdot \{87\} \bmod \{11b\} = (1\ 0000\ 1110) \bmod \{11b\}$$

$$= (1\ 0000\ 1110) \text{ xor } (1\ 0001\ 1011) = (0001\ 0101)$$

Mix Columns

- can express each col as 4 equations
 - to derive each new byte in col
- decryption requires use of inverse matrix
 - with larger coefficients, hence a little harder
- have an alternate characterisation
 - each column a 4-term polynomial
 - with coefficients in $GF(2^8)$
 - and polynomials multiplied modulo (x^4+1)
- coefficients based on linear code with maximal distance between codewords

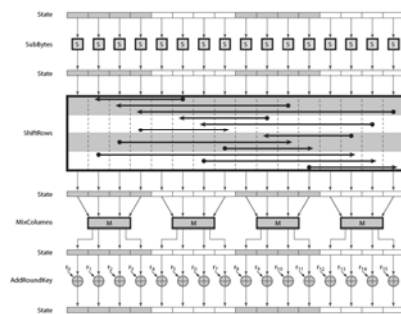
Add Round Key

- XOR state with 128-bits of the round key
- again processed by column (though effectively a series of byte operations)
- inverse for decryption identical
 - since XOR own inverse, with reversed keys
- designed to be as simple as possible
 - a form of Vernam cipher on expanded key
 - requires other stages for complexity / security

Add Round Key



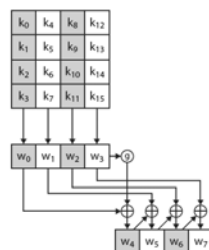
AES Round



AES Key Expansion

- takes 128-bit (16-byte) key and expands into array of 44/52/60 32-bit words
- start by copying key into first 4 words
- then loop creating words that depend on values in previous & 4 places back
 - in 3 of 4 cases just XOR these together
 - 1st word in 4 has rotate + S-box + XOR round constant on previous, before XOR 4th back

AES Key Expansion



Key Expansion Rationale

- designed to resist known attacks
- design criteria included
 - knowing part key insufficient to find many more
 - invertible transformation
 - fast on wide range of CPU's
 - use round constants to break symmetry
 - diffuse key bits into round keys
 - enough non-linearity to hinder analysis
 - simplicity of description

Implementation Aspects

- can efficiently implement on 32-bit CPU
 - redefine steps to use 32-bit words
 - can precompute 4 tables of 256-words
 - then each column in each round can be computed using 4 table lookups + 4 XORs
 - at a cost of 4Kb to store tables
- designers believe this very efficient implementation was a key factor in its selection as the AES cipher

Summary

- have considered:
 - the AES selection process
 - the details of Rijndael – the AES cipher
 - looked at the steps in each round
 - the key expansion
 - implementation aspects