# GPS Free Node Localization in Mobile Wireless Sensor Networks

5th ACM international workshop on Data engineering for wireless and mobile access

Year of Publication: 2006

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## Background

#### Purpose of Localization Schemes

- Optimized or maintained connectivity
- Coordination for node tasks

#### Localization can require GPS

- GPS signal not always available
- Indoors, GPS unreliable

#### Fixed Point reference nodes

- Use of beacons
- Static network

## Paper Contributions

"The main contribution of this work is that it presents a solution to the problem of directional localization in GPS free sensor networks with mobile nodes."

- Provides directional neighbor localization in a networkwide coordinate system
- Works under fairly large motion and distance measurement errors
- Unaffected by the speed of nodes
- Works for any network size
- Supports a stable network in mobility problems

#### **Assumptions**

- Each node has a compass pointing North (or any other common reference direction)
- Nodes can measure the distance to their neighbors using a well known range measurement method (e.g. Time of Arrival (TOA))
- Motion actuators allow each node to move a specific distance in a specific direction.
- Actuator, compass and distance measurements are subject to errors caused by various real world disturbances
- Other than the above, no additional positioning equipment or infrastructure is required.

The core localization algorithm works on well defined rounds. Each round essentially consists of three steps:

- 1. Measure distances between neighbors
- 2. Move nodes
- 3. Exchange distance values for that round as validation for movement

#### **Core Localization Algorithm**

```
CoreLocalization(n_1, n_2, v_1, \alpha_1)

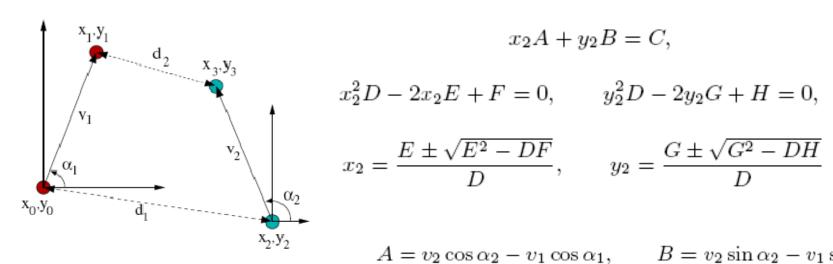
1: d_1 \leftarrow \text{inter-distance}(n_1, n_2)

2: Move node n_1 by v_1 and \alpha_1

3: d_2 \leftarrow \text{inter-distance}(n_1, n_2)

4: Retrieve v_2 and \alpha_2 from n_2

5: Calculate positions of n_2 using equations (4),(5) and (6)
```



 $x_3 = x_2 + v_2 \cos \alpha_2,$   $y_3 = y_2 + v_2 \sin \alpha_2,$ 

 $(x_3 - x_1)^2 + (y_3 - y_1)^2 = d_2^2, x_2^2 + y_2^2 = d_1^2.$ 

 $x_1 = v_1 \cos \alpha_1$ ,

 $y_1 = v_1 \sin \alpha_1,$ 

$$x_2A + y_2B = C, (4)$$

$$x_2^2 D - 2x_2 E + F = 0,$$
  $y_2^2 D - 2y_2 G + H = 0,$  (5)

$$x_2 = \frac{E \pm \sqrt{E^2 - DF}}{D}, \qquad y_2 = \frac{G \pm \sqrt{G^2 - DH}}{D}$$
 (6)

$$A = v_2 \cos \alpha_2 - v_1 \cos \alpha_1, \qquad B = v_2 \sin \alpha_2 - v_1 \sin \alpha_1,$$

$$C = \frac{1}{2} \left( d_2^2 - d_1^2 - v_1^2 - v_2^2 + 2v_1v_2\cos(\alpha_1 - \alpha_2) \right).$$

$$D = A^{2} + B^{2},$$
  $E = AC,$   $F = C^{2} - d_{1}^{2}B^{2},$   $G = BC,$   $H = C^{2} - d_{1}^{2}A^{2}.$ 

#### **Verification Algorithm**

```
VERIFICATION(NEIGHBORLIST NL)

1: for each neighbor pair (m, n) in NL do

2: if m and n are neighbors then

3: d_{m,n} \leftarrow measured inter-distance(m, n)

4: for each position pair \{m^i, n^j \mid i, j = 1, 2\} do

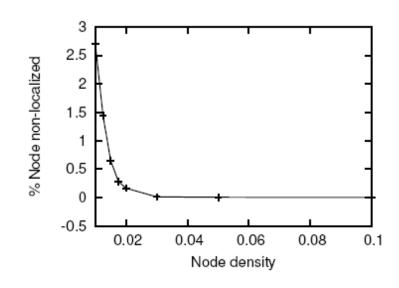
5: Compute Euclidean distance D between m^i and n^j

6: if D = d_{m,n} then

7: mark m^i and n^j as exact positions
```

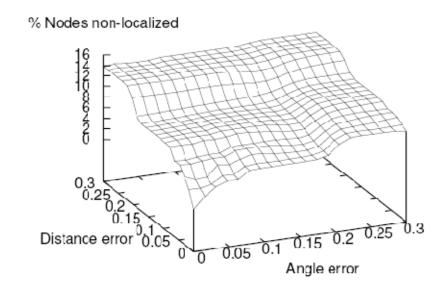
#### **Ideal Conditions**

- Placed nodes in a 100x100 area
- Each simulation is run for 100 rounds
- Random walk, random speed
- As small as 3% maximum failure for very sparse networks



## **Including Measurement Errors**

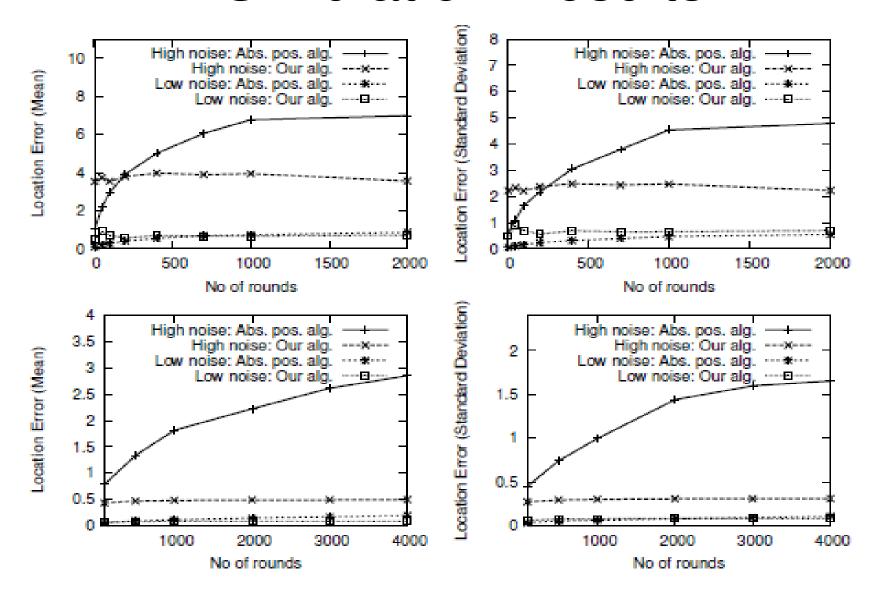
- Same as previous experiment
- Distance noise as a percent of measured value
- Angle noise as a static % of 2 pi



#### Comparison with an absolute positioning algorithm

- Units are placed with initially perfect data and record their own movement from there
- Performed random movement and directed movement experiments
- 2000 rounds, averaged error at 6 places

		Our alg.		Abs. pos. alg.	
Movement	Noise	Mean	Stdev	Mean	Stdev
Random	low	0.71	0.69	0.86	0.55
	$_{ m high}$	3.55	2.23	6.98	4.78
Directed	low	0.08	0.08	0.19	0.11
	high	0.49	0.30	2.85	1.65



## Strength And Weakness

#### Strengths:

- Localization without the use of GPS.
- Does not require any infrastructure
- Information about relative position.
- Gives error in the range of 3m.

#### Weakness:

- Need of compass at each node.
- Cannot give the location information in terms of coordinates.
- Comparison of algorithm with an absolute positioning algorithm whose name has not been mentioned.

## Paper Significance to Project

Useful for relative localization of nodes.

 Can be used at instance as no infrastructure is required.

GPS for our project?

# Algorithms for Nodes Localization in Wireless Ad-Hoc Networks Based on Cost Function

International Workshop on Wireless Ad- Hoc Networks(IWWAN)

Year of Publication: 2005

#### Introduction

 Distribute algorithm to localize sensor network nodes.

Use of UWB for accuracy.

 Based on capacity of nodes to calculate Time of arrival(TOA) and Angle of Arrival(AOA).

## **Algorithm**

1. Determine Node beacon distances

2. Compute the cost function of every node.

 Compute the coordinate of the node using Davidson-Fletcher-Powell Quasi Newton algorithm (DFP) or Direct Method(DM) algorithm.

#### Relative Position Estimation

Shortest Path Estimation:

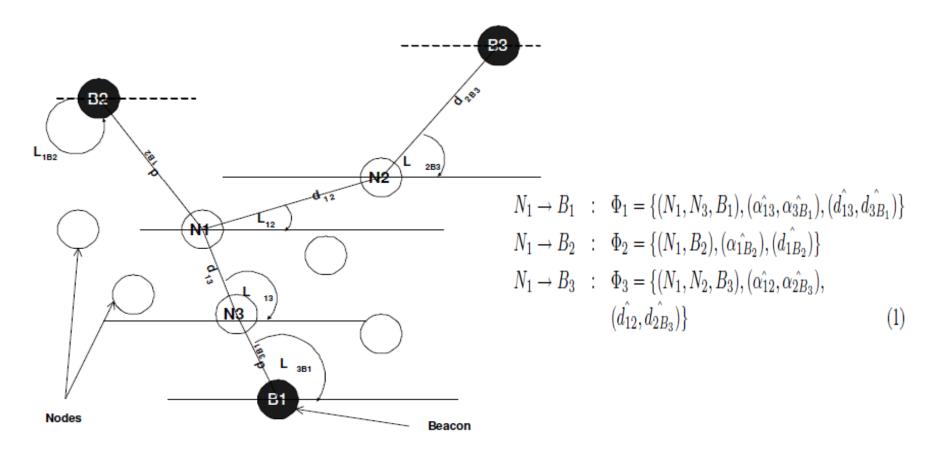


Fig. 1. Scheme of Wireless Sensor Network

#### Relative Position Estimation

Position Estimation:

Cost Function a estimated angle,

distance between nodes,

no. of beacons,

no. of hops between a node and the given beacon

$$\mathbf{E}(x,y) = \sum_{k=1}^{N_B} \left( \sqrt{\left( x_k - \left( x_k + \sum_{i=1}^{N_{hop}(k)} \hat{d}_i \cdot \cos(\hat{\alpha}_i) \right) \right)^2 + \left( y_k - \left( y_k + \sum_{i=1}^{N_{hop}(k)} \hat{d}_i \cdot \sin(\hat{\alpha}_i) \right) \right)^2} - \sqrt{\left( x_k - x \right)^2 + \left( y_k - y \right)^2} \right)^2$$

## Positioning Algorithm

- Davidson-Fletcher-Powell Quasi Newton algorithm (DFP):
  - Gives position vector using the following equation:

$$f(p) = \sum_{i=1}^{N_B} \left[ \sqrt{(x_e - x_i)^2 + (y_e - y_i)^2} - \hat{d}_{ei} \right]^2$$

$$\mathbf{p} = [x, y]^{\mathsf{T}}.$$

## Positioning Algorithm

Direct Method:

$$f(p) = \sum_{i=1}^{N_B} \left[ \sqrt{(x_e - x_i)^2 + (y_e - y_i)^2} - \hat{d}_{ei} \right]^2$$

$$\begin{pmatrix} x_e \\ y_e \end{pmatrix} = \begin{pmatrix} a_1 & b_1 \\ a_2 & b_2 \end{pmatrix}^{-1} \cdot \begin{pmatrix} g_1 \\ g_2 \end{pmatrix}$$

 Results show that algorithm is more sensitive to TOA than to AOA.

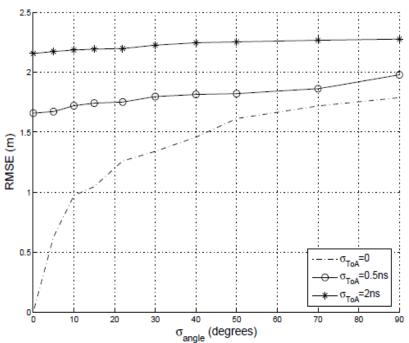


Fig. 2. Root Mean Squared error of position estimation with Direct Method. Only 5 beacons are chosen to position all the sensor nodes in the WSN. Three different values of the variance on the ToA error are chosen ( $\sigma_{ToA} = \{0, 0.6, 2\}$ ns).

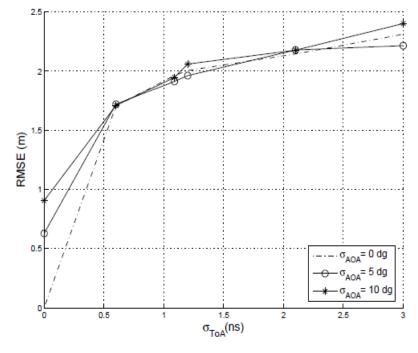


Fig. 4. Root Mean Squared error of position estimation with Direct Method. Only 5 beacons are chosen to position all the sensor nodes in the WSN. Three different values of the variance on the AoA error are chosen ( $\sigma_{AoA} = \{0, 5, 10\}$  degrees).

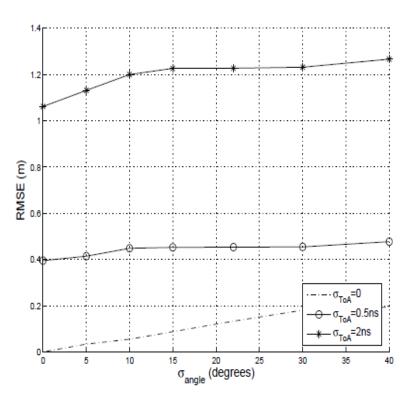


Fig. 3. Root Mean Squared error of position estimation with DFP algorithm. Only 5 beacons are chosen to position all the sensor nodes in the WSN. Three different values of the variance on the ToA error are chosen ( $\sigma_{ToA} = \{0, 0.6, 2\}$ ns).

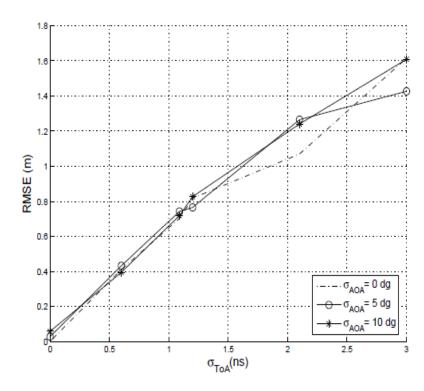


Fig. 5. Root Mean Squared error of position estimation with Direct Method. Only 5 beacons are chosen to position all the sensor nodes in the WSN. Three different values of the variance on the AoA error are chosen ( $\sigma_{AoA} = \{0,5,10\}$  degrees).

DFP is positionally more accurate than DM

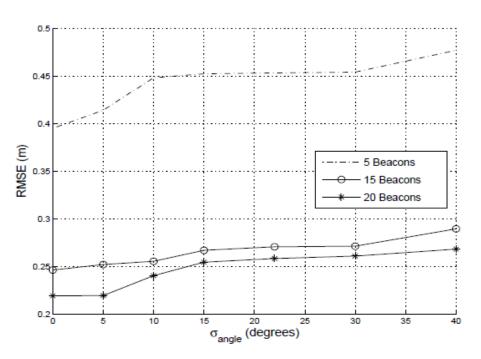


Fig. 6. Root Mean Squared error of position estimation with DFP using 5, 15 and 20 beacons. The  $\sigma_{ToA}$  is equal to 0, 5 ns.

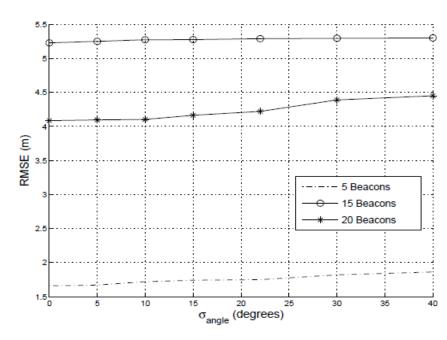


Fig. 7. Root Mean Squared error of position estimation with DM using 5, 15 and 20 beacons. The  $\sigma_{ToA}$  is equal to 0, 5 ns.

## Strengths and Weakness

#### Strengths:

- Gives exact position along with coordinates of node with error of about 1.3 meters.
- Distributed algorithm.
- No use of GPS and use of UWB.
- No extra devices or instruments needed on the node.

## Strengths and Weakness

#### Weakness:

- Algorithm not compared with other existing algorithms.
- Need of beacons along with their coordinates to estimate the position of nodes.
- Depends upon the density of beacons for accuracy.

## Paper Significance to the Project

Doesn't rely on GPS

 Useful in determining the location with exact coordinates.