

**CIS6930 Mathematics for Intelligent Systems II Spring 2009**

**Home Work Assignment 2: Due Thursday 03/05/09 before class**

1. Prove that the second variation (i.e., the second differential) of a twice differentiable functional is unique.
2. Show that the hyperbolic set  $\{x \in \mathbb{R}_+^n \mid \prod_{i=1}^n x_i \geq 1\}$  is *convex*.
3. If  $f : \mathbb{R}^n \rightarrow \mathbb{R}$ , then the *perspective* of  $f$  is the function  $g : \mathbb{R}^{n+1} \rightarrow \mathbb{R}$  defined by  $g(x, t) = tf(x/t)$ , with the domain  $\text{dom } g = \{(x, t) \mid x/t \in \text{dom } f, t > 0\}$ . Prove that if  $f$  is a convex function so is  $g$ .
4. Write the dual formulation for the SVM with slack variables discussed in class.
5. Prove that if  $K(x, y)$  is a valid kernel function then so is  $(K(x, y))^2$ .