#### Binary Tree Traversal Methods





- In a traversal of a binary tree, each element of the binary tree is visited exactly once.
- During the visit of an element, all action (make a clone, display, evaluate the operator, etc.) with respect to this element is taken.

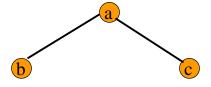
## Binary Tree Traversal Methods

- Preorder
- Inorder
- Postorder
- Level order

### Preorder Traversal

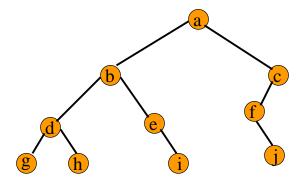
```
public static void preOrder(BinaryTreeNode t)
{
    if (t != null)
    {
       visit(t);
       preOrder(t.leftChild);
       preOrder(t.rightChild);
    }
}
```

## Preorder Example (visit = print)



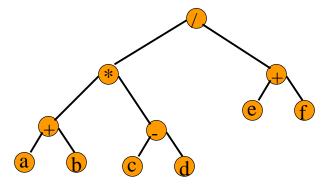
a b c

# Preorder Example (visit = print)



abdgheicfj

## Preorder Of Expression Tree



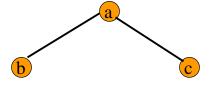
/ \* + a b - c d + e f

Gives prefix form of expression!

### **Inorder Traversal**

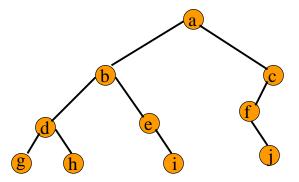
```
public static void inOrder(BinaryTreeNode t)
{
    if (t != null)
    {
        inOrder(t.leftChild);
        visit(t);
        inOrder(t.rightChild);
    }
}
```

## Inorder Example (visit = print)



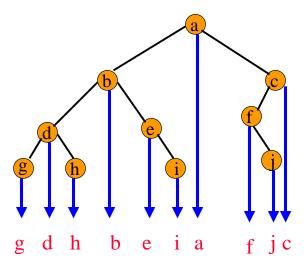
b a c

## Inorder Example (visit = print)

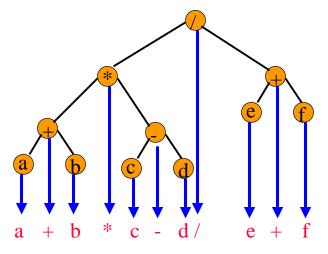


gdhbeiafjc

## Inorder By Projection (Squishing)



# Inorder Of Expression Tree

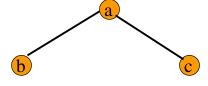


Gives infix form of expression (sans parentheses)!

### Postorder Traversal

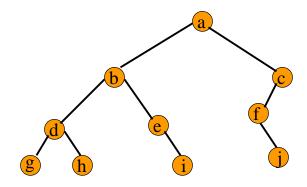
```
public static void postOrder(BinaryTreeNode t)
{
    if (t != null)
        {
            postOrder(t.leftChild);
            postOrder(t.rightChild);
            visit(t);
        }
}
```

## Postorder Example (visit = print)



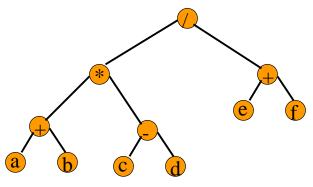
b c a

# Postorder Example (visit = print)



ghdi ebj fca

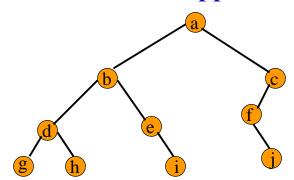
## Postorder Of Expression Tree



a b + c d - \* e f + /

Gives postfix form of expression!

## **Traversal Applications**

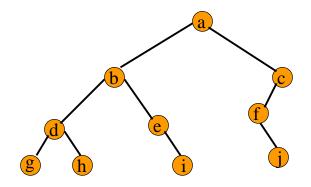


- Make a clone.
- Determine height.
- •Determine number of nodes.

#### Level Order

```
Let t be the tree root.
while (t != null)
{
    visit t and put its children on a FIFO queue;
    remove a node from the FIFO queue and
    call it t;
    // remove returns null when queue is empty
}
```

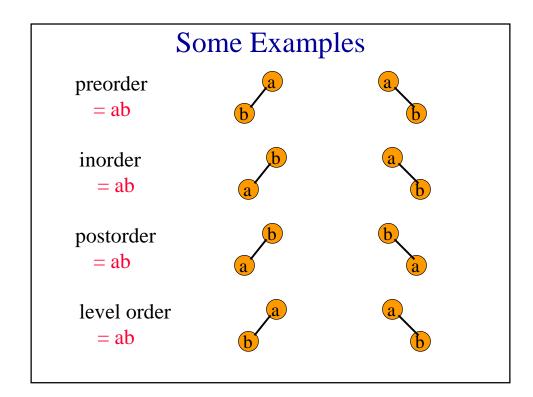
## Level-Order Example (visit = print)



abcdefghij

### **Binary Tree Construction**

- Suppose that the elements in a binary tree are distinct.
- Can you construct the binary tree from which a given traversal sequence came?
- When a traversal sequence has more than one element, the binary tree is not uniquely defined.
- Therefore, the tree from which the sequence was obtained cannot be reconstructed uniquely.



### **Binary Tree Construction**

- Can you construct the binary tree, given two traversal sequences?
- Depends on which two sequences are given.

#### Preorder And Postorder

preorder = abpostorder = ba

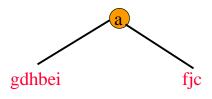




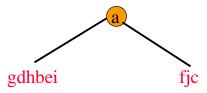
- Preorder and postorder do not uniquely define a binary tree.
- Nor do preorder and level order (same example).
- Nor do postorder and level order (same example).

#### **Inorder And Preorder**

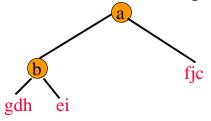
- inorder = g d h b e i a f j c
- preorder = a b d g h e i c f j
- Scan the preorder left to right using the inorder to separate left and right subtrees.
- a is the root of the tree; gdhbei are in the left subtree; fjc are in the right subtree.



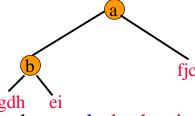
#### Inorder And Preorder



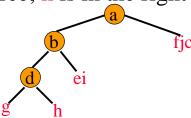
- preorder = a b d g h e i c f j
- b is the next root; gdh are in the left subtree; ei are in the right subtree.



#### **Inorder And Preorder**



- preorder = a b d g h e i c f j
- d is the next root; g is in the left subtree; h is in the right subtree.



#### Inorder And Postorder

- Scan postorder from right to left using inorder to separate left and right subtrees.
- inorder = g d h b e i a f j c
- postorder = g h d i e b j f c a
- Tree root is a; gdhbei are in left subtree; fjc are in right subtree.

#### Inorder And Level Order

- Scan level order from left to right using inorder to separate left and right subtrees.
- inorder = g d h b e i a f j c
- level order = a b c d e f g h i j
- Tree root is a; gdhbei are in left subtree; fjc are in right subtree.