



## Queues

- Linear list.
- One end is called **front**.
- Other end is called **rear**.
- Additions are done at the **rear** only.
- Removals are made from the **front** only.

## Bus Stop Queue



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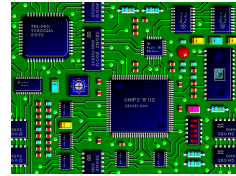
## The Interface Queue

```
public interface Queue
{
    public boolean isEmpty();
    public Object getFrontEelement();
    public Object getRearEelement();
    public void put(Object theObject);
    public Object remove();
}
```

## Revisit Of Stack Applications

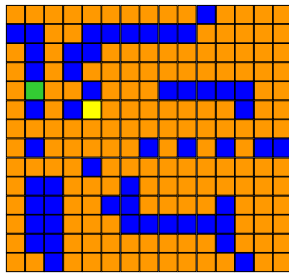
- Applications in which the stack cannot be replaced with a queue.
  - Parentheses matching.
  - Towers of Hanoi.
  - Switchbox routing.
  - Method invocation and return.
  - Try-catch-throw implementation.
- Application in which the stack may be replaced with a queue.
  - Rat in a maze.
    - Results in finding shortest path to exit.

## Wire Routing



### Lee's Wire Router

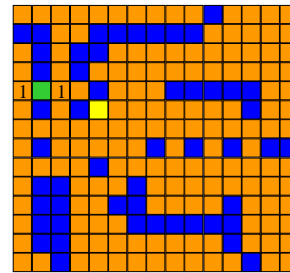
- start pin
- end pin



Label all reachable squares **1** unit from start.

### Lee's Wire Router

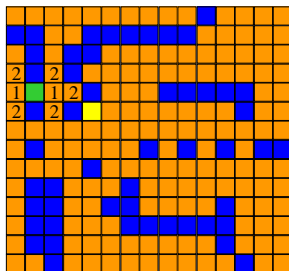
- start pin
- end pin



Label all reachable unlabeled squares **2** units from start.

### Lee's Wire Router

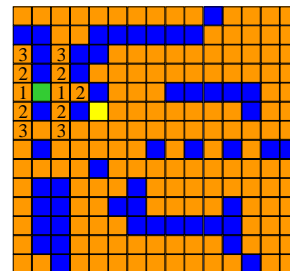
- start pin
- end pin



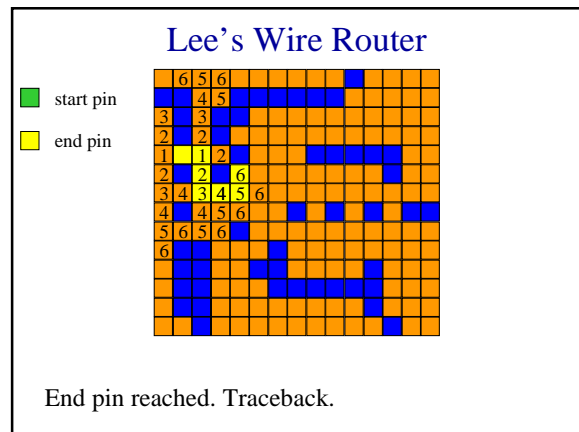
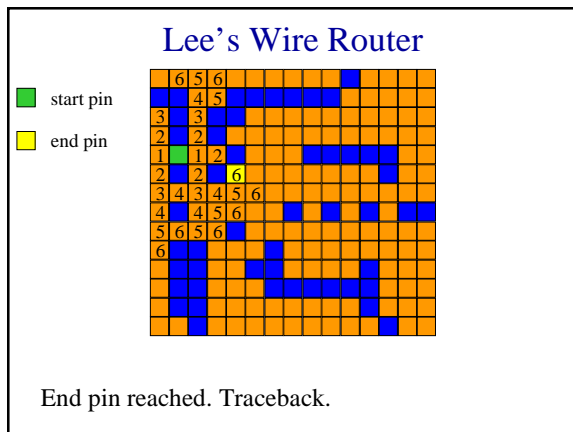
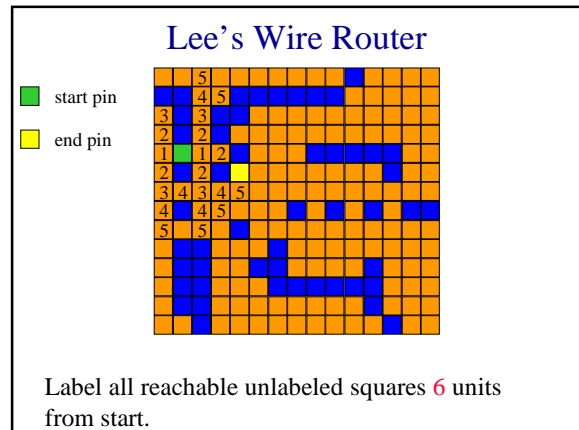
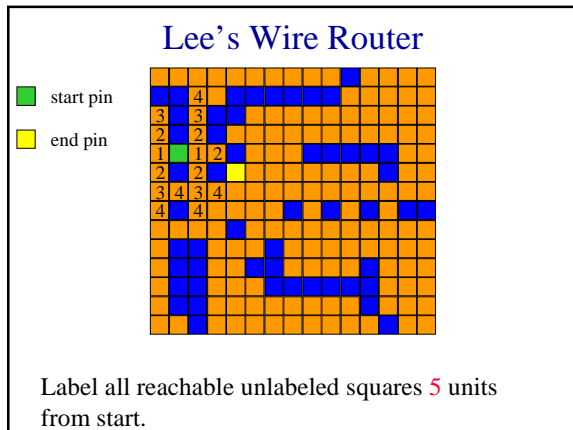
Label all reachable unlabeled squares **3** units from start.

### Lee's Wire Router

- start pin
- end pin



Label all reachable unlabeled squares **4** units from start.



### Derive From ArrayLinearList

a	b	c	d	e															
0	1	2	3	4	5	6													

➤ when front is left end of list and rear is right end

- Queue.isEmpty() => super.isEmpty()  
– O(1) time
- getFrontElement() => get(0)  
– O(1) time
- getRearElement() => get(size() - 1)  
– O(1) time
- put(theObject) => add(size(), theObject)  
– O(1) time
- remove() => remove(0)  
– O(size) time

### Derive From ArrayLinearList

e	d	c	b	a															
0	1	2	3	4	5	6													

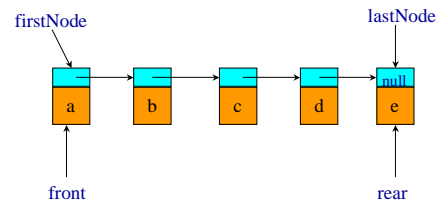
▪ when rear is left end of list and front is right end

- Queue.isEmpty() => super.isEmpty()  
– O(1) time
- getFrontElement() => get(size() - 1)  
– O(1) time
- getRearElement() => get(0)  
– O(1) time
- put(theObject) => add(0, theObject)  
– O(size) time
- remove() => remove(size() - 1)  
– O(1) time

## Derive From ArrayLinearList

- to perform each operation in  $O(1)$  time (excluding array doubling), we need a customized array representation.

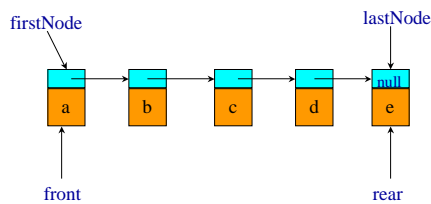
## Derive From ExtendedChain



➤ when front is left end of list and rear is right end

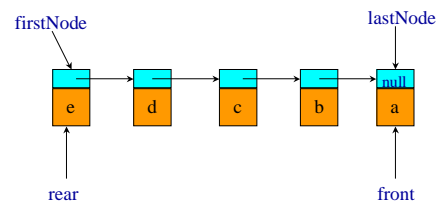
- `Queue.isEmpty()` => `super.isEmpty()`  
–  $O(1)$  time
- `getFrontElement()` => `get(0)`  
–  $O(1)$  time

## Derive From ExtendedChain



- `getRearElement()` => `getLast()` ... new method  
–  $O(1)$  time
- `put(theObject)` => `append(theObject)`  
–  $O(1)$  time
- `remove()` => `remove(0)`  
–  $O(1)$  time

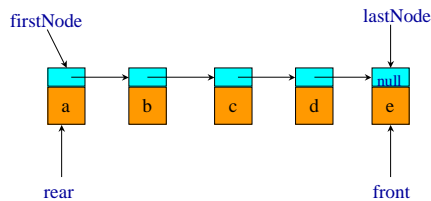
## Derive From ExtendedChain



➤ when front is right end of list and rear is left end

- `Queue.isEmpty()` => `super.isEmpty()`  
–  $O(1)$  time
- `getFrontElement()` => `getLast()`  
–  $O(1)$  time

## Derive From ExtendedChain



- `getRearElement()` => `get(0)`  
–  $O(1)$  time
- `put(theObject)` => `add(0, theObject)`  
–  $O(1)$  time
- `remove()` => `remove(size-1)`  
–  $O(\text{size})$  time

## Custom Linked Code

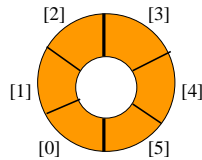
- Develop a linked class for **Queue** from scratch to get better performance than obtainable by deriving from **ExtendedChain**.

## Custom Array Queue

- Use a 1D array `queue`.

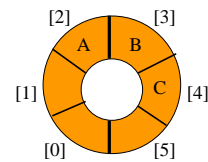
`queue[]` 

- Circular view of array.



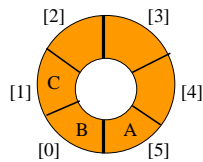
## Custom Array Queue

- Possible configuration with 3 elements.



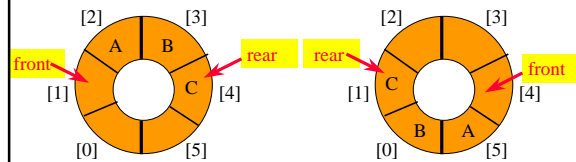
## Custom Array Queue

- Another possible configuration with 3 elements.



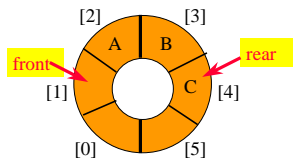
## Custom Array Queue

- Use integer variables `front` and `rear`.
  - `front` is one position counterclockwise from first element
  - `rear` gives position of last element



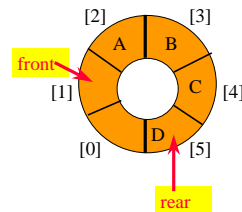
## Add An Element

- Move `rear` one clockwise.



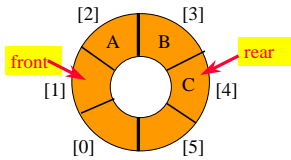
## Add An Element

- Move `rear` one clockwise.
- Then put into `queue[rear]`.



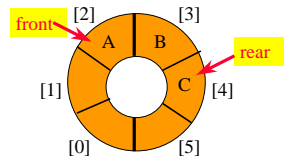
## Remove An Element

- Move **front** one clockwise.



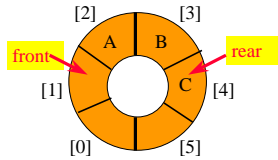
## Remove An Element

- Move **front** one clockwise.
- Then extract from **queue[front]**.



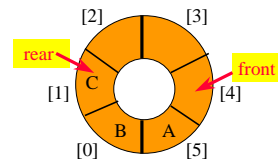
## Moving rear Clockwise

- rear++;**
- if (rear == queue.length) rear = 0;**

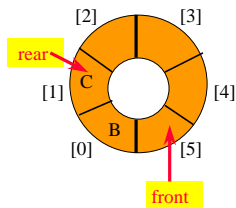


- rear = (rear + 1) % queue.length;**

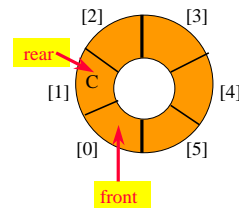
## Empty That Queue



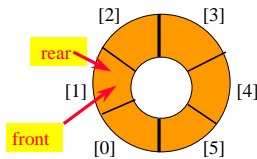
## Empty That Queue



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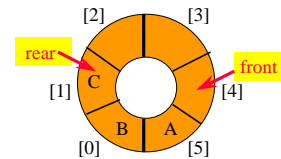


### Empty That Queue

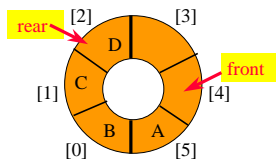


- When a series of removes causes the queue to become empty,  $\text{front} = \text{rear}$ .
- When a queue is constructed, it is empty.
- So initialize  $\text{front} = \text{rear} = 0$ .

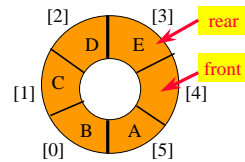
### A Full Tank Please



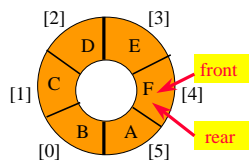
### A Full Tank Please



### A Full Tank Please



### A Full Tank Please



- When a series of adds causes the queue to become full,  $\text{front} = \text{rear}$ .
- So we cannot distinguish between a full queue and an empty queue!

### Ouch!!!!

- Remedies.
  - Don't let the queue get full.
    - When the addition of an element will cause the queue to be full, increase array size.
    - This is what the text does.
  - Define a boolean variable  $\text{lastOperationIsPut}$ .
    - Following each **put** set this variable to **true**.
    - Following each **remove** set to **false**.
    - Queue is empty iff  $(\text{front} == \text{rear}) \ \&\& \ !\text{lastOperationIsPut}$
    - Queue is full iff  $(\text{front} == \text{rear}) \ \&\& \ \text{lastOperationIsPut}$

## Ouch!!!!

- Remedies (continued).
  - Define an integer variable `size`.
    - Following each `put` do `size++`.
    - Following each `remove` do `size--`.
    - Queue is empty iff (`size == 0`)
    - Queue is full iff (`size == queue.length`)
  - Performance is slightly better when first strategy is used.