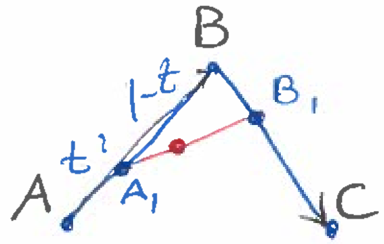


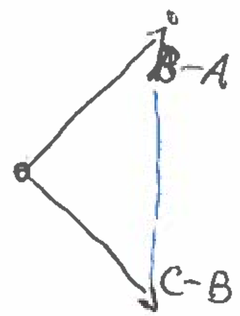
$t = \frac{1}{3}$

$n=2$

$$p(t) := A(1-t)^2 + B\,2(1-t)t + Ct^2$$

$$= \underbrace{\left(\underbrace{A(1-t)+Bt}_{A_1}\right)(1-t) + \left(\underbrace{B(1-t)+Ct}_{B_1}\right)t}$$

$$= A_1 (1-t) + B_1 t$$



$\times 2$

$$p'(t) = 2\left[B(1-t) - A(1-t) + Ct - Bt\right]$$

$$= 2\left[(B-A)(1-t) + (C-B)t\right]$$

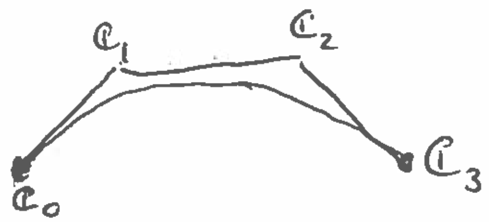
$i+j=n$

j

Bezier form: $b_i^n(t) := \frac{n!}{(n-i)!\,i!}\underbrace{(1-t)}_{s}^{n-i} t^i$ $\quad s+t=1$

basis

$n=3$



$$p_3(t) := \sum c_i\, b_i^3(t)$$

$$p_3(0) = c_0 \qquad b_i^3(0) = \begin{cases} 0 & \text{else} \\ 1 & i=0 \end{cases}$$

1^{st} difference

$$p(t) = \sum c_i\, b_i^3(t)$$

$$p'(t) = 3\left(\sum \underbrace{(c_{j+1} - c_j)}\, b_j^2(t)\right)$$

"one"

$$p''(t) = 3\cdot 2\left(\sum (c_{k+2} - 2c_{k+1} + c_k)\, b_k^1(t)\right)$$

2^{nd} difference

$$\underbrace{(c_{k+2} - c_{k+1}) - (c_{k+1} - c_k)}$$

$$c_{k+2} - 2c_{k+1} + c_k$$

$1 \quad -2 \quad 1$

$\cancel{w_1 (1-t)^2}$

$$\int c_0 (1-t)^2 + c_1 2t(1-t) + c_2 t^2$$

$$= \sum_{i=0}^{2} c_i/3$$

$$\int \sum_{i=0}^{n} c_i \, b_i^n(t)$$

$$= \sum_{i=0}^{n} c_i/n$$

$$* \int_0^1 (1-t)^2 = \frac{1}{3}$$

$$* \int_0^1 2t(1-t) = \frac{1}{3}$$

$$* \int_0^1 t^2 = \frac{1}{3}$$

<u>BB-Form</u> $\int \left(\frac{n!}{(n-i)!\,i!}\right)(1-t)^{n-i} t^i = \frac{1}{n}$