#### Rank

Rank of an element is its position in ascending key order.

[2,6,7,8,10,15,18,20,25,30,35,40]

rank(2) = 0

rank(15) = 5

rank(20) = 7

### **Selection Problem**

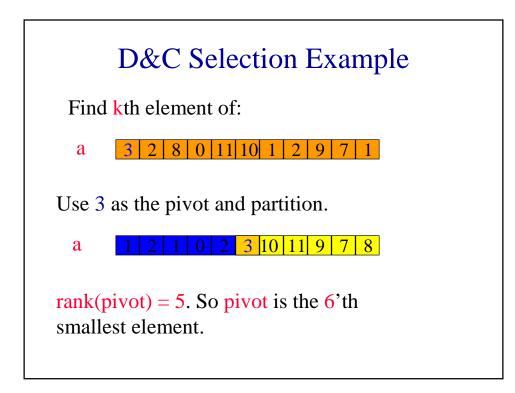
- Given n unsorted elements, determine the k'th smallest element. That is, determine the element whose rank is k-1.
- Applications
  - Median score on a test.
    - k = ceil(n/2).
  - Median salary of Computer Scientists.
  - Identify people whose salary is in the bottom 10%. First find salary at the 10% rank.

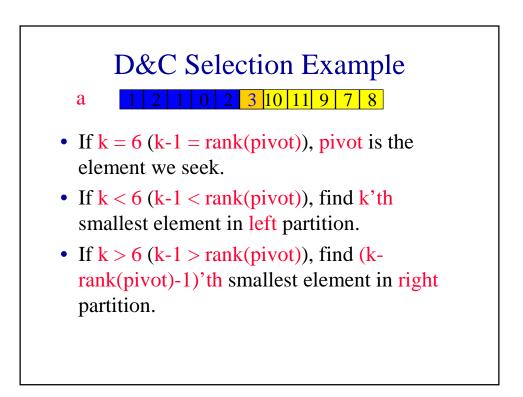
# Selection By Sorting

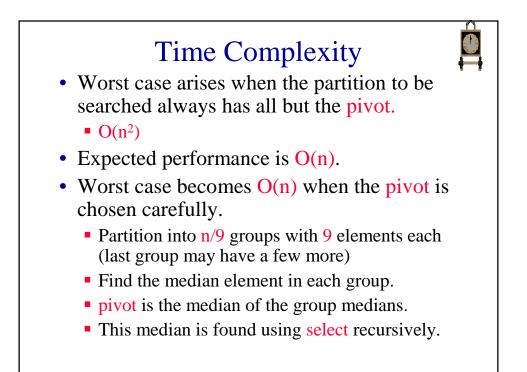
- Sort the **n** elements.
- Pick up the element with desired rank.
- O(n log n) time.

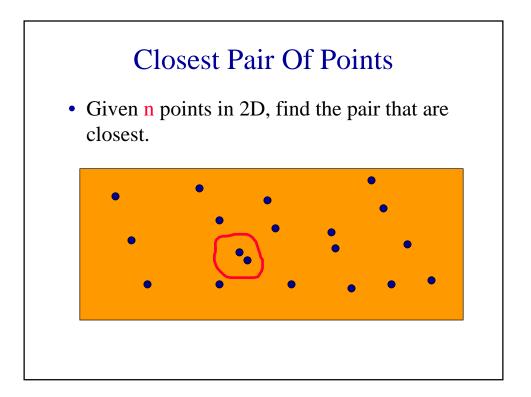
#### **Divide-And-Conquer Selection**

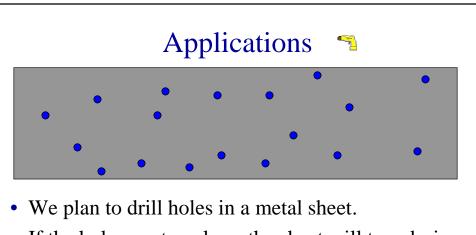
- Small instance has n <= 1. Selection is easy.
- When n > 1, select a pivot element from out of the n elements.
- Partition the n elements into 3 groups left, middle and right as is done in quick sort.
- The rank of the pivot is the location of the pivot following the partitioning.
- If k-1 = rank(pivot), pivot is the desired element.
- If k-1 < rank(pivot), determine the k'th smallest element in left.
- If k-1 > rank(pivot), determine the (k-rank(pivot)-1)'th smallest element in right.



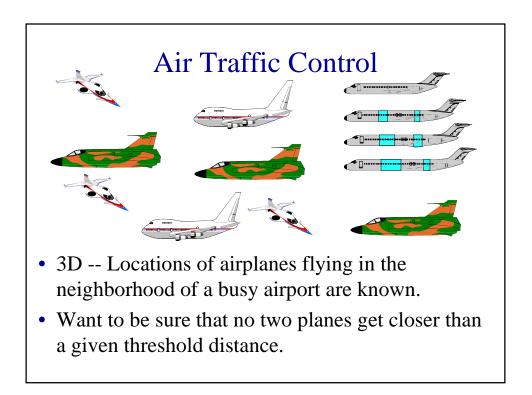








- If the holes are too close, the sheet will tear during drilling.
- Verify that no two holes are closer than a threshold distance (e.g., holes are at least 1 inch apart).



# Simple Solution

- For each of the n(n-1)/2 pairs of points, determine the distance between the points in the pair.
- Determine the pair with the minimum distance.
- **O**(n<sup>2</sup>) time.



- When **n** is small, use simple solution.
- When **n** is large
  - Divide the point set into two roughly equal parts A and B.
  - Determine the closest pair of points in A.
  - Determine the closest pair of points in **B**.
  - Determine the closest pair of points such that one point is in A and the other in B.
  - From the three closest pairs computed, select the one with least distance.

