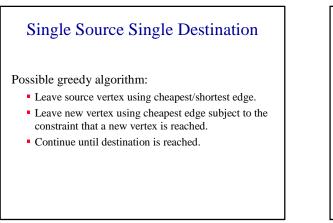
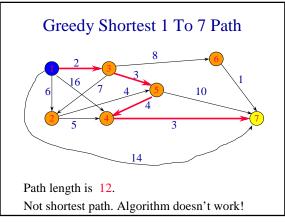




- Single source single destination.
- Single source all destinations.
- All pairs (every vertex is a source and destination).



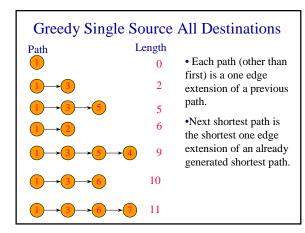


Single Source All Destinations

Need to generate up to **n** (**n** is number of vertices) paths (including path from source to itself).

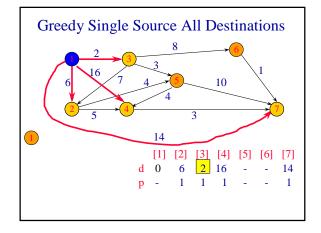
Greedy method:

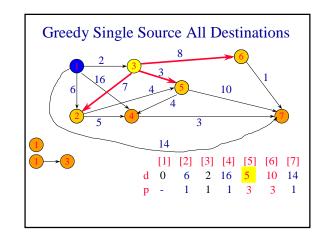
- Construct these up to **n** paths in order of increasing length.
- Assume edge costs (lengths) are ≥ 0 .
- So, no path has length < 0.
- First shortest path is from the source vertex to itself. The length of this path is 0.

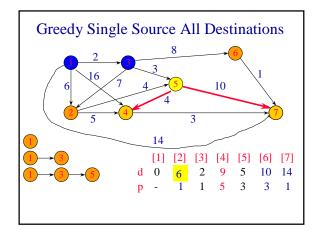


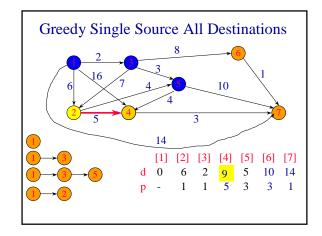
Greedy Single Source All Destinations

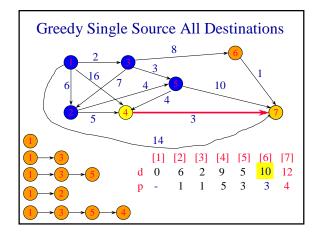
- Let d(i) (distanceFromSource(i)) be the length of a shortest one edge extension of an already generated shortest path, the one edge extension ends at vertex i.
- The next shortest path is to an as yet unreached vertex for which the d() value is least.
- Let p(i) (predecessor(i)) be the vertex just before vertex i on the shortest one edge extension to i.

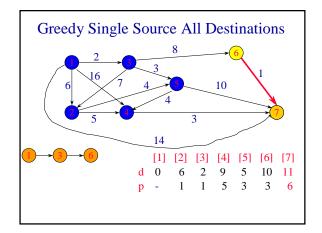


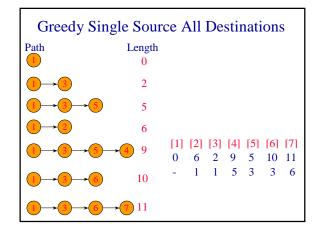


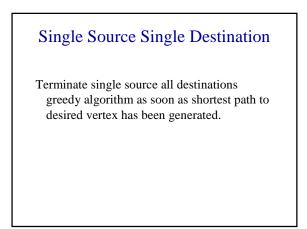










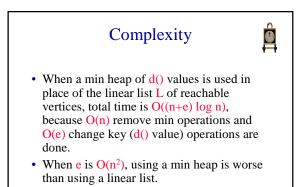


Data Structures For Dijkstra's Algorithm

- The greedy single source all destinations algorithm is known as Dijkstra's algorithm.
- Implement d() and p() as 1D arrays.
- Keep a linear list L of reachable vertices to which shortest path is yet to be generated.
- Select and remove vertex v in L that has smallest d() value.
- Update d() and p() values of vertices adjacent to v.

Complexity

- O(n) to select next destination vertex.
- O(out-degree) to update d() and p() values when adjacency lists are used.
- O(n) to update d() and p() values when adjacency matrix is used.
- Selection and update done once for each vertex to which a shortest path is found.
- Total time is $O(n^2 + e) = O(n^2)$.



• When a Fibonacci heap is used, the total time is $O(n \log n + e)$.