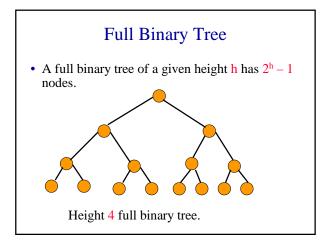
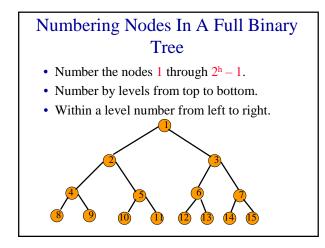
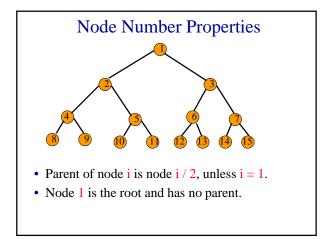


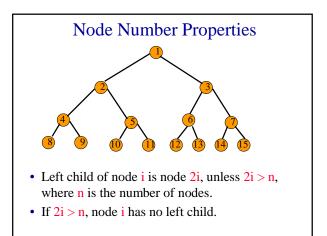
Number Of Nodes & Height

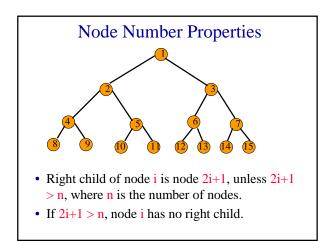
- Let **n** be the number of nodes in a binary tree whose height is **h**.
- $h \le n \le 2^h 1$
- $\log_2(n+1) \le h \le n$





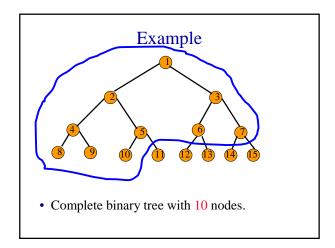






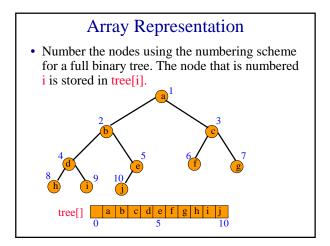
Complete Binary Tree With n Nodes

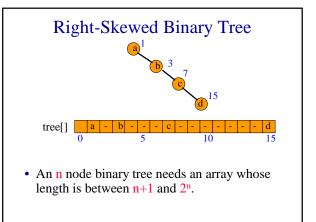
- Start with a full binary tree that has at least n nodes.
- Number the nodes as described earlier.
- The binary tree defined by the nodes numbered 1 through n is the unique n node complete binary tree.



Binary Tree Representation

- Array representation.
- Linked representation.





Linked Representation

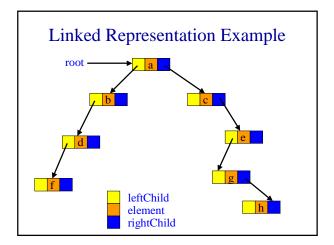
- Each binary tree node is represented as an object whose data type is **BinaryTreeNode**.
- The space required by an **n** node binary tree is n * (space required by one node).

The Class BinaryTreeNode

package dataStructures; public class BinaryTreeNode Object element; BinaryTreeNode leftChild; // left subtree BinaryTreeNode rightChild;// right subtree // constructors and any other methods // come here

{

}



Some Binary Tree Operations

- Determine the height.
- Determine the number of nodes.
- Make a clone.
- Determine if two binary trees are clones.
- Display the binary tree.
- Evaluate the arithmetic expression represented by a binary tree.
- Obtain the infix form of an expression.
- Obtain the prefix form of an expression.
- Obtain the postfix form of an expression.

Binary Tree Traversal

- Many binary tree operations are done by performing a traversal of the binary tree.
- In a traversal, each element of the binary tree is visited exactly once.
- During the visit of an element, all action (make a clone, display, evaluate the operator, etc.) with respect to this element is taken.

Binary Tree Traversal Methods

- Preorder
- Inorder
- Postorder
- Level order