## Queues



- Linear list.
- One end is called front.
- Other end is called rear.
- Additions are done at the rear only.
- Removals are made from the front only.


## Bus Stop Queue



## Bus Stop Queue


front


Bus Stop Queue


## Bus Stop Queue



## The Interface Queue

public interface Queue
public boolean isEmpty();
public Object getFrontEelement(); public Object getRearEelement();
public void put(Object theObject);
public Object remove();
\}

## Revisit Of Stack Applications

- Applications in which the stack cannot be replaced with a queue.
- Parentheses matching.
- Towers of Hanoi.
- Switchbox routing.
- Method invocation and return.
- Try-catch-throw implementation.
- Application in which the stack may be replaced with a queue.
- Rat in a maze.
- Results in finding shortest path to exit.


## Wire Routing




Label all reachable unlabeled squares 2 units from start.


Label all reachable unlabeled squares 3 units from start.


Label all reachable unlabeled squares 4 units from start.


Label all reachable unlabeled squares 5 units from start.


Label all reachable unlabeled squares 6 units from start.


End pin reached. Traceback.

| ee's Wire Router |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| start pin |  | 6 | 5 | 6 |  |  |  |  |  |  |  |
|  |  |  | 4 | 5 |  |  |  |  |  |  |  |
|  | 3 |  | 3 |  |  |  |  |  |  |  |  |
| end pin | 2 |  | 2 |  |  |  |  |  |  |  |  |
|  | 12 |  | 1 | 2 |  |  |  |  |  |  |  |
|  | 2 |  | 2 |  | 6 |  |  |  |  |  |  |
|  | 3 | 4 | 3 | 4 | 5 | 6 |  |  |  |  |  |
|  | 4 |  | 4 | 5 | 6 |  |  |  |  |  |  |
|  | 5 | 6 | 5 | 6 |  |  |  |  |  |  |  |
|  | 6 |  |  |  |  |  |  |  |  |  |  |
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|  |  |  |  |  |  |  |  |  |  |  |  |

End pin reached. Traceback.

## Derive From ArrayLinearList


$\begin{array}{lllllll}0 & 1 & 2 & 3 & 4 & 5 & 6\end{array}$
$>$ when front is left end of list and rear is right end

- Queue.isEmpty() => super.isEmpty()
- O(1) time
- getFrontElement ()$=>\operatorname{get}(0)$
- O(1) time
- getRearElement() $=>\operatorname{get}(\operatorname{size}()-1)$
- O(1) time
- put(theObject) $=>$ add(size () , theObject $)$
- O(1) time
- remove() => remove(0)
- O(size) time


## Derive From ArrayLinearList


$\begin{array}{lllllll}0 & 1 & 2 & 3 & 4 & 5 & 6\end{array}$

- when rear is left end of list and front is right end
- Queue.isEmpty() => super.isEmpty()
- O(1) time
- getFrontElement() $=>\operatorname{get}(\operatorname{size}()-1)$
- O(1) time
- getRearElement() => get $(0)$
- O(1) time
- put(theObject) $=>\operatorname{add}(0$, theObject $)$
- O(size) time
- remove ()$=>\operatorname{remove}(\operatorname{size}()-1)$
- O(1) time


## Derive From ArrayLinearList

- to perform each opertion in $\mathrm{O}(1)$ time (excluding array doubling), we need a customized array representation.


## Derive From ExtendedChain


when front is left end of list and rear is right end

- Queue.isEmpty() => super.isEmpty()
- O(1) time
- getFrontElement( $)=>\operatorname{get}(0)$
- O(1) time



## Derive From ExtendedChain


when front is right end of list and rear is left end

- Queue.isEmpty() => super.isEmpty()
- O(1) time
- getFrontElement() => getLast()
- O(1) time



## Custom Linked Code

- Develop a linked class for Queue from scratch to get better preformance than obtainable by deriving from ExtendedChain.


## Custom Array Queue

- Use a 1D array queue.

```
queue[] [|||||
```

- Circular view of array.



## Custom Array Queue

- Possible configuration with 3 elements.



## Custom Array Queue

- Another possible configuration with 3 elements.



## Custom Array Queue

- Use integer variables front and rear.
- front is one position counterclockwise from first element
- rear gives position of last element



## Add An Element

- Move rear one clockwise.



## Add An Element

- Move rear one clockwise.
- Then put into queue[rear].



## Remove An Element

- Move front one clockwise.



## Remove An Element

- Move front one clockwise.
- Then extract from queue[front].



## Moving rear Clockwise

- rear++;
if (rear $==$ queue.length) rear $=0$;

- rear $=($ rear +1$) \%$ queue.length;


## Empty That Queue



## Empty That Queue



## Empty That Queue



## Empty That Queue



- When a series of removes causes the queue to become empty, front = rear.
- When a queue is constructed, it is empty.
- So initialize front $=$ rear $=0$.


## A Full Tank Please



A Full Tank Please


A Full Tank Please


## A Full Tank Please



- When a series of adds causes the queue to become full, front = rear.
- So we cannot distinguish between a full queue and an empty queue!


## Ouch!!!!!

- Remedies.
- Don't let the queue get full.
- When the addition of an element will cause the queue to be full, increase array size.
- This is what the text does.
- Define a boolean variable lastOperationIsPut.
- Following each put set this variable to true.
- Following each remove set to false.
- Queue is empty iff (front $==$ rear) \&\& !lastOperationIsPut
- Queue is full iff (front $==$ rear) \& \& lastOperationIsPut


## Ouch!!!!!

- Remedies (continued).
- Define an integer variable size.
- Following each put do size++.
- Following each remove do size--.
- Queue is empty iff (size $==0$ )
- Queue is full iff (size == queue.length)
- Performance is slightly better when first strategy is used.

