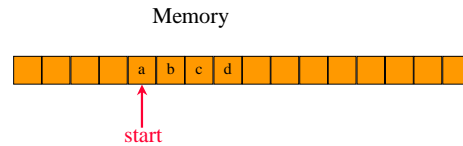


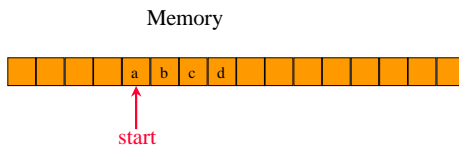


1D Array Representation In Java, C, and C++



- 1-dimensional array $x = [a, b, c, d]$
- map into contiguous memory locations
- $\text{location}(x[i]) = \text{start} + i$

Space Overhead



space overhead = 4 bytes for **start**
 + 4 bytes for **x.length**
 = 8 bytes
 (excludes space needed for the elements of **x**)

2D Arrays

The elements of a 2-dimensional array **a** declared as:

```
int [][]a = new int[3][4];
```

may be shown as a table

a[0][0]	a[0][1]	a[0][2]	a[0][3]
a[1][0]	a[1][1]	a[1][2]	a[1][3]
a[2][0]	a[2][1]	a[2][2]	a[2][3]

Rows Of A 2D Array

a[0][0]	a[0][1]	a[0][2]	a[0][3]	→ row 0
a[1][0]	a[1][1]	a[1][2]	a[1][3]	→ row 1
a[2][0]	a[2][1]	a[2][2]	a[2][3]	→ row 2

Columns Of A 2D Array

a[0][0]	a[0][1]	a[0][2]	a[0][3]
a[1][0]	a[1][1]	a[1][2]	a[1][3]
a[2][0]	a[2][1]	a[2][2]	a[2][3]
↓	↓	↓	↓
column 0	column 1	column 2	column 3

2D Array Representation In Java, C, and C++

2-dimensional array x

a, b, c, d
e, f, g, h
i, j, k, l

view 2D array as a 1D array of rows

$x = [\text{row0}, \text{row1}, \text{row2}]$

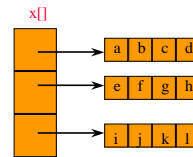
row 0 = [a, b, c, d]

row 1 = [e, f, g, h]

row 2 = [i, j, k, l]

and store as 4 1D arrays

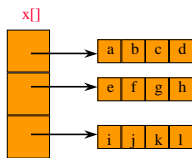
2D Array Representation In Java, C, and C++



$x.\text{length} = 3$

$x[0].\text{length} = x[1].\text{length} = x[2].\text{length} = 4$

Space Overhead



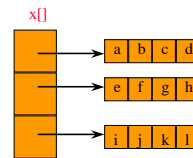
space overhead = overhead for 4 1D arrays

= $4 * 8$ bytes

= 32 bytes

= (number of rows + 1) x 8 bytes

Array Representation In Java, C, and C++



- This representation is called the **array-of-arrays** representation.
- Requires contiguous memory of size 3, 4, 4, and 4 for the 4 1D arrays.
- 1 memory block of size **number of rows** and **number of rows** blocks of size **number of columns**

Row-Major Mapping

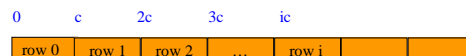
- Example 3 x 4 array:

a b c d
e f g h
i j k l

- Convert into 1D array y by collecting elements by rows.
- Within a row elements are collected from left to right.
- Rows are collected from top to bottom.
- We get $y[] = \{a, b, c, d, e, f, g, h, i, j, k, l\}$



Locating Element $x[i][j]$



- assume x has r rows and c columns
- each row has c elements
- i rows to the left of row i
- so ic elements to the left of $x[i][0]$
- so $x[i][j]$ is mapped to position $ic + j$ of the 1D array

Space Overhead

row 0	row 1	row 2	...	row i		
-------	-------	-------	-----	-------	--	--

4 bytes for **start** of 1D array +
4 bytes for **length** of 1D array +
4 bytes for **c** (number of columns)
= 12 bytes

(number of rows = **length** / **c**)

Disadvantage

Need contiguous memory of size **rc**.

Column-Major Mapping

a b c d

e f g h

i j k l

- Convert into 1D array **y** by collecting elements by columns.
- Within a column elements are collected from top to bottom.
- Columns are collected from left to right.
- We get **y** = {a, e, i, b, f, j, c, g, k, d, h, l}

Matrix

Table of values. Has rows and columns, but numbering begins at 1 rather than 0.

a b c d row 1

e f g h row 2

i j k l row 3

- Use notation **x(i,j)** rather than **x[i][j]**.
- May use a 2D array to represent a matrix.

Shortcomings Of Using A 2D Array For A Matrix

- Indexes are off by 1.
- Java arrays do not support matrix operations such as **add**, **transpose**, **multiply**, and so on.
 - Suppose that **x** and **y** are 2D arrays. Can't do **x + y**, **x - y**, **x * y**, etc. in Java.
- Develop a class **Matrix** for object-oriented support of all matrix operations. See text.

Diagonal Matrix

An **n x n** matrix in which all nonzero terms are on the diagonal.

Diagonal Matrix

```

1 0 0 0
0 2 0 0
0 0 3 0
0 0 0 4

```

- $x(i,j)$ is on diagonal iff $i = j$
- number of diagonal elements in an $n \times n$ matrix is n
- non diagonal elements are zero
- store diagonal only vs n^2 whole

Lower Triangular Matrix

An $n \times n$ matrix in which all nonzero terms are either on or below the diagonal.

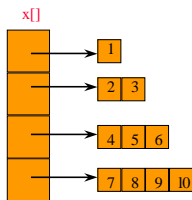
```

1 0 0 0
2 3 0 0
4 5 6 0
7 8 9 10

```

- $x(i,j)$ is part of lower triangle iff $i \geq j$.
- number of elements in lower triangle is $1 + 2 + \dots + n = n(n+1)/2$.
- store only the lower triangle

Array Of Arrays Representation



Use an irregular 2-D array ... length of rows is not required to be the same.

Creating And Using An Irregular Array

```

// declare a two-dimensional array variable
// and allocate the desired number of rows
int [][] irregularArray = new int [numberOfRows][];

// now allocate space for the elements in each row
for (int i = 0; i < numberOfRows; i++)
    irregularArray[i] = new int [size[i]];

// use the array like any regular array
irregularArray[2][3] = 5;
irregularArray[4][6] = irregularArray[2][3] + 2;
irregularArray[1][1] += 3;

```

Map Lower Triangular Array Into A 1D Array

Use row-major order, but omit terms that are not part of the lower triangle.

For the matrix

```

1 0 0 0
2 3 0 0
4 5 6 0
7 8 9 10

```

we get

1, 2, 3, 4, 5, 6, 7, 8, 9, 10

Index Of Element $[i][j]$



- Order is: row 1, row 2, row 3, ...
- Row i is preceded by rows 1, 2, ..., $i-1$
- Size of row i is i .
- Number of elements that precede row i is $1 + 2 + 3 + \dots + i-1 = i(i-1)/2$
- So element (i,j) is at position $i(i-1)/2 + j - 1$ of the 1D array.