



Data Structures



data object

set or collection of instances

$\text{integer} = \{0, +1, -1, +2, -2, +3, -3, \dots\}$

$\text{daysOfWeek} = \{\text{S}, \text{M}, \text{T}, \text{W}, \text{Th}, \text{F}, \text{Sa}\}$

Data Object

instances may or may not be related

$\text{myDataObject} = \{\text{apple}, \text{chair}, 2, 5.2, \text{red}, \text{green}, \text{Jack}\}$



Data Structure



Data object +
relationships that exist among instances
and elements that comprise an instance

Among instances of integer

$369 < 370$

$280 + 4 = 284$



Data Structure



Among elements that comprise an instance

369

3 is more significant than 6

3 is immediately to the left of 6

9 is immediately to the right of 6

Data Structure

The relationships are usually specified by specifying operations on one or more instances.

add, subtract, predecessor, multiply

Linear (or Ordered) Lists

instances are of the form

$(e_0, e_1, e_2, \dots, e_{n-1})$

where e_i denotes a list element

$n \geq 0$ is finite

list size is n

Linear Lists

$L = (e_0, e_1, e_2, e_3, \dots, e_{n-1})$

relationships

e_0 is the zero'th (or front) element

e_{n-1} is the last element

e_i immediately precedes e_{i+1}

Linear List Examples/Instances

Students in COP3530 =

(Jack, Jill, Abe, Henry, Mary, ..., Judy)

Exams in COP3530 =

(exam1, exam2, exam3)

Days of Week = (S, M, T, W, Th, F, Sa)

Months = (Jan, Feb, Mar, Apr, ..., Nov, Dec)

Linear List Operations—size()

determine list size

$L = (a, b, c, d, e)$

size = 5

Linear List Operations—get(theIndex)

get element with given index

$L = (a, b, c, d, e)$

$get(0) = a$

$get(2) = c$

$get(4) = e$

$get(-1) = \text{error}$

$get(9) = \text{error}$

Linear List Operations— indexOf(theElement)

determine the index of an element

$L = (a, b, d, b, a)$

$indexOf(d) = 2$

$indexOf(a) = 0$

$indexOf(z) = -1$

Linear List Operations— remove(theIndex)

remove and return element with given index

$L = (a, b, c, d, e, f, g)$

$remove(2)$ returns c

and L becomes (a, b, d, e, f, g)

index of d, e, f , and g decrease by 1

Linear List Operations— remove(theIndex)

remove and return element with given
index

$L = (a, b, c, d, e, f, g)$

$remove(-1) \Rightarrow \text{error}$

$remove(20) \Rightarrow \text{error}$

Linear List Operations— add(theIndex, theElement)

add an element so that the new element has
a specified index

$L = (a, b, c, d, e, f, g)$

$add(0, h) \Rightarrow L = (h, a, b, c, d, e, f, g)$

index of a, b, c, d, e, f and g increase by 1

Linear List Operations— add(theIndex, theElement)

$L = (a, b, c, d, e, f, g)$

$add(2, h) \Rightarrow L = (a, b, h, c, d, e, f, g)$

index of c, d, e, f and g increase by 1

$add(10, h) \Rightarrow \text{error}$

$add(-6, h) \Rightarrow \text{error}$

Data Structure Specification

❑ Language independent

➤ Abstract Data Type

❑ Java

➤ Interface

➤ Abstract Class

Linear List Abstract Data Type

```
AbstractDataType LinearList
{
  instances
    ordered finite collections of zero or more elements
  operations
    isEmpty(): return true iff the list is empty, false otherwise
    size(): return the list size (i.e., number of elements in the list)
    get(index): return the indexth element of the list
    indexOf(x): return the index of the first occurrence of x in
      the list, return -1 if x is not in the list
    remove(index): remove and return the indexth element,
      elements with higher index have their index reduced by 1
    add(theIndex, x): insert x as the indexth element, elements
      with theIndex >= index have their index increased by 1
    output(): output the list elements from left to right
}
```

Linear List as Java Interface

An interface may include constants and abstract methods (i.e., methods for which no implementation is provided).

Linear List as Java Interface

```
public interface LinearList
{
    public boolean isEmpty();
    public int size();
    public Object get(int index);
    public int indexOf(Object elem);
    public Object remove(int index);
    public void add(int index, Object obj);
    public String toString();
}
```

Implementing An Interface

```
public class ArrayLinearList implements LinearList
{
    // code for all LinearList methods must be provided here
}
```

Linear List As An Abstract Class

An abstract class may include constants, variables, abstract methods, and nonabstract methods.

Linear List As Java Abstract Class

```
public abstract class LinearListAsAbstractClass
{
    public abstract boolean isEmpty();
    public abstract int size();
    public abstract Object get(int index);
    public abstract int indexOf(Object theElement);
    public abstract Object remove(int index);
    public abstract void add(int index,
                           Object theElement);
    public abstract String toString();
}
```

Extending A Java Class

```
public class ArrayLinearList
    extends LinearListAsAbstractClass
{
    // code for all abstract classes must come here
}
```

Implementing Many Interfaces

```
public class MyInteger implements Operable, Zero,
                                CloneableObject
{
    // code for all methods of Operable, Zero,
    // and CloneableObject must be provided
}
```



Extending Many Classes



NOT PERMITTED IN JAVA

A Java class may implement as many interfaces as it wants but can extend at most 1 class.



Data Structures In Text



All but 1 of our data structures are specified as Java interfaces.

Exception is *Graph* in Chapter 17.

Java specifies all of its data structures as interfaces.

java.util.List